Republic of Zambia
Ministry of Education, Science, Vocational Training and Early Education

# "O" Level Mathematics Syllabus 

Grades 10 to 12


Published by the Curriculum development Centre
P. O. Box 50092

Lusaka
MAY 2013

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Quality, lifelong education for all which is accessible, inclusive and relevant to individual, national and global needs and value systems.

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## PREFACE

The syllabus was produced as a result of the Curriculum review process carried out by the Ministry of Education, Science, Vocational Training and Early Education under the auspices of the Curriculum Development Centre (CDC). The curriculum reform process started way back in 1999 when the Ministry of Education commissioned five (5) curriculum studies which were conducted by the University of Zambia. These studies were followed by a review of the lower and middle basic and primary teacher education curriculum. In 2005 the upper basic education National survey was conducted and information from learners, parents, teachers, school managers, educational administrators, tertiary institutions traditional leaders civic leaders and various stakeholders in education was collected to help design a relevant curriculum.

The recommendations provided by various stakeholders during the Upper Basic Education National survey of 2005 and National symposium on curriculum held in June 2009 guided the review process.

The review was necessitated by the need to provide an education system that would not only incorporate latest social, economic, technological and political developments but also equip learners with vital knowledge, skills and values that are necessary to contribute to the attainment of Vision 2030.

The syllabus has been reviewed in line with the Outcome Based Education principles which seek to link education to real life experiences that give learners skills to access, criticize analyse and practically apply knowledge that help them gain life skills. Its competences and general outcomes are the expected outcomes to be attained by the leaners through the acquisition of knowledge, skills, techniques and values which are very important for the total development of the individual and the nation as a whole.

Effective implementation of Outcome Based Education requires that the following principles be observed: clarity of focus, Reflective designing, setting high expectations for all learners and appropriate opportunities.

It is my sincere hope that this Outcome Based syllabus will greatly improve the quality of education provided at Grade 10 to 12 level as defined and recommended in various policy documents including Educating Our Future`1996 and the `Zambia Education Curriculum Framework `2013.

Chishimba Nkosha
Permanent Secretary
MINISTRY OF EDUCATION,SCIENCE, VOCATIONAL TRAINING AND EARLY EDUCATION.

## Acknowledgement

The syllabus presented here is a result of broad-based consultation involving several stakeholders within and outside the education system.
Many individuals, institutions and organizations were consulted to gather their views on the existing syllabus and to accord them an opportunity to make suggestions for the new syllabus. The Ministry of Education wishes to express heartfelt gratitude to all those who participated for their valuable contributions, which resulted in the development of this syllabus.

The Curriculum Development Centre worked closely with other sister departments and institutions to create this document. We sincerely thank the Directorate of Teacher Education and Specialized Services, the Directorate of Planning and Information, the Directorate of Human Resource and Administration, the Directorate of Open and Distance Education ,the Examinations Council of Zambia, the University of Zambia, schools and other institutions too numerous to mention, for their steadfast support.

We pay special tribute to co-operating partners especially JICA and UNICEF for rendering financial technical support in the production of the syllabus.
C.N.M Sakala (Mrs)

Director-Standard and Curriculum
MINISTRY OF EDUCATION, SCIENCE,VOCATIONAL TRAINING AND EARLY EDUCATION

## Introduction

## Suggested Teaching Methodology

- The syllabus encourages a learner-centred approach or pedagogy. This involves learners to learn Mathematics in context of multipart, comprehensive and practical problems. Under such learning situations learners may be put in groups and required to identify what they already know, what they need to know and how and where to access new information that may lead to resolution of the problem.
- The Problem-Based Learning (PBL) in mathematics may include the four core area specific outcomes, thinking process, skills and values with the aim of nurturing wise citizens who are responsible in decision-making for sustainable and responsible development.
- The role of the teacher may be that of a facilitator of learning who provides appropriate scaffolding of that process by asking probing questions, providing appropriate resources and leading class discussions as well as designing student's assessments. The strategy strives to transform the traditional teacher centred mathematics classroom situation into student centred environment completely where learners are allowed to construct new knowledge through, the specific outcomes learned, thinking processes such as communication, interconnections, reasoning, representations, problem solving and other similar ones: both mathematics and non-mathematical positive as well as universal values.
- The teaching of Ordinary Level Mathematics should expose learners to practical applications of mathematics in everyday life. Learners should be exposed to do more of practical work as much as necessary through contextual reference to the local environment.
- use of computer related software for mathematics should be encouraged and the teacher should encourage learners to use available mathematics software.
- Learners may be exposed to situation where they can provide assistance and support to their peer in learning groups. The opportunities may help to evaluate their peers and conduct self-assessment that helps them to shoulder responsibility for their learning.


## Time and Period allocation

Time allocation for this syllabus is will require at seven-40 minutes periods per week to complete.

## Assessment Scheme

Continuous assessment will be emphasised by using various methods of testing according to topics and themes at various levels. The examinations council of Zambia will prepare detailed procedures on how continuous assessment will be conducted by the teachers. The Examinations Council will also develop examination syllabus to provide teachers with guidelines on the objectives to be tested. The scheme of assessment will consists of school based assessment and final examination that will be conducted by the Examinations Council of Zambia.

School based assessment will be in the form of tests. Tests will be in the form of diagnostic, aptitude, achievement, oral, practice, attitude and performance, exercises, assignments, discussions, investigation, project work etc. School based assessment shall contribute towards certification of all learners.

## Rationale

Mathematics is an important tool for the development and improvement of a person's intellectual competence in logical reasoning, spatial visualization, analysis and abstract thought. When learners have acquired enough knowledge in mathematics they develop numeracy, reasoning, thinking skill and problem solving skills. Mathematics is very important not only in science and technology that is vital for the development of the country but also in everyday life and workplace. Mathematics would equip the learner to live in modern age of Science and technology and enable the learner to contribute to the social and economic development of the country and the world at large. Mathematics plays a vital role in the development of highly skilled and technologically based manpower. Mathematics also prepares and enhances the learners' prospect of employment and further education as it also plays a key role as a tool for other learning areas and subject. Mathematics relates to all subjects and provides necessary mathematical pre-requisites for further education. Other subjects in science and technology heavily depend on mathematics concepts. In order for Zambia to comfortably reach the 2010 millennium goals there has to be a deliberate emphasis on mathematics education.

Mathematics can also be an interesting subject as it can also be a subject of enjoyment and excitement. This offers learners and students an opportunity for creative work and moments of joy and pleasure. It is very interesting for students and indeed all learners when they discover ideas and insights that would help them pursue mathematics even outside school walls.

The study of mathematics will build up understanding and appreciation of basic mathematical concepts and computational skills in order to apply them in everyday life. Mathematics aims at developing clear mathematical thinking and expression in a learner and also develop ability to recognize problem and to solve them with related mathematical knowledge and skills.

Through the study of mathematics learners will develop ethical values necessary for accountability in financial matters. It will develop in them the skills of interpreting and financial information. It will help learners acquire skills for planning, budgeting and effective decision-making.

## General Outcomes

- To build an understanding and appreciation of basic mathematical concepts and computational skills in order to apply them in everyday life.
- Through the study of mathematics learners will develop ethical values necessary for accountability in financial matters. It will develop in them the skills of interpreting and financial information. It will help learners acquire skills for planning, budgeting and effective decisionmaking.


## GRADE 10

## General Outcomes

- Provide clear mathematical thinking and expression in the learner
- Develop the learners' mathematical knowledge and skills
- Enrich the learners' understanding of mathematical concepts in order to facilitate further study of the discipline
- Build up an appreciation of mathematical concepts so that the learner can apply these for problem solving in everyday life.
- Enable the learner represent, interpret and use data in a variety of forms
- Inculcate a desire to develop different career paths in the learners


## Key Competences

- Assimilate necessary mathematical concepts for use in everyday life such as environment and other related disciplines
- Thank mathematically and accurately in problem solving skills and apply these skills to formulate and solve mathematical and other related problems.
- Develop necessary skills needed to apply mathematical concepts and skills in other disciplines.
- Produce imaginative and creative work from mathematical concepts and ideas.
- Develop abilities and ideas drawn from mathematics to reason logically, communicate mathematically, and learn independently without too much supervision (selfdiscipline).
- Development positive attitudes towards mathematics and use it in other subjects such as science and technology.
- Apply mathematical tools such as information and communication technology in the learning of other subjects.
- Use mathematics for enjoyment and pleasure
- Develop understanding of algebra, geometry, measurements and shapes.

| TOPIC | SUBTOPICS | SPECIFIC OUTCOMES | KNOWLEDGE | SKILLS | VALUES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10.2 SETS | 10.2.1 Set Operations | 10.2.1.1 Carry out operations on sets. <br> 10.2.1.2 Apply higher operations on sets | - Operations on sets. <br> - Numerical problems involving sets <br> - Applying higher operations on sets (numerical problems involving sets ) | - Identification of operations on sets <br> - Comparing numerical problems involving sets <br> - Computations involving sets. | - Appreciation of set operations. <br> - Curiosity in computations. |
| 10.3 INDEX <br>  NOTATION | 10.3.1 Indices | 10.1.5.1 Apply laws of <br> indices <br> 10.1.5.2 Simplify positive, <br> negative and zero indices <br> 10.1.5.3 Simplify fractional <br> indices <br> 10.1.5.4 Solve equations <br> involving indices | - Laws of indices <br> - Double indices <br> - Multiplicative inverse <br> - Fractions with negative indices <br> - Equations involving indices <br> - Problems involving application of indices | - Identification of indices with same base. <br> - Simplification using indices. <br> - Application of indices to simplify multiplication and division. | - Curiosity in using indices to solve problems. <br> - Appreciation of using indices. <br> - Logical thinking in simplifying using indices. |
| 10.4 ALGEBRA | 10.3.1 Basic <br>  Processes | 10.3.1.1 Expand and simplify expressions <br> 10.3.1.3 Factorise algebraic expressions <br> 10.3.1.5 Simplify Algebraic fractions | - Expansion and simplification of expressions <br> - Factorisation by using common factors, grouping terms, factors of quadratic expressions and difference of two square <br> - Addition , subtraction , | - Simplification of expressions <br> - Identification of common factors, factors of quadratic expressions and difference of two square <br> - Computation of | - Orderliness in factorisation of algebraic expressions <br> - Logical thinking in factorising quadratics. |


| TOPIC | SUBTOPICS | SPECIFIC OUTCOMES | KNOWLEDGE | SKILLS | VALUES |
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|  |  |  | multiplication and division of algebraic fractions <br> - Lowest common multiple | algebraic fractions applying the four rules. |  |
| 10.5 MATRICES | 10.5.1 Transpose of a matrix <br> 10.5.2 Multiplicatio n of matrices <br> 10.5.3 Inverse of a matrix | 10.5.1.1Find a Transpose of a matrix <br> 10.5.2.1 Multiply matrices (up to $3 \times 3$ matrices) <br> 10.5.2.2 Calculate the determinant of a 2 by 2 matrix <br> 10.5.3. 1 Find the inverse of a 2 by 2 matrix <br> 10.5.3.1 Solve systems of linear equations in two variables <br> 10.5.3.2Apply matrices to solve real life problems | - Transpose of a matrix <br> - Multiplying matrices (up to $3 \times 3$ matrices) <br> - The null (zero) and identity matrices <br> - Determinant and Inverse of a $2 \times 2$ matrix <br> - Singular matrices <br> - Solving systems of linear equation in two variables using matrices <br> - Cramer's Rule <br> - Applying matrices to solve real life problems | - Interpretation of transpose of a matrix. <br> - Comparison of matrices. <br> - Computation of matrices <br> - Application of matrices in solving linear equations. | - Appreciation of matrices. <br> - Awareness of solving linear equations using matrices. |
| 10.6 SIMILARITY AND CONGRUENC Y | 10.6.1 Application <br> of Ratio and <br> Proportion <br> 10.6.2 Areas and <br>  Volumes of <br>  <br> Similar <br>  figures | 10.6.2.1 Calculate the scale on a map <br> 10.6.2.2 Calculate length and area using a given scale and vice versa <br> 10.6.2.3 Calculate areas and volumes of similar figures <br> 10.6.2.4 Apply ratio, proportion, to solve problems on similarity and congruence | - Representative Fraction (Scale) <br> - Calculating length and area using a given scale and vice versa <br> - Calculating areas and volumes of similar figures <br> - Applying ratio, proportion, similarity and congruence in solving real life problems | - Computation of representative fractions (RFs). <br> - Representation of measurements on the map. <br> - Application of ratio, proportion, similarity and congruence in solving real life problems | - Judgement of virtual and actual distances <br> - Accuracy in computation |


| TOPIC |  | SUBTOPICS |  | SPECIFIC OUTCOMES |  | KNOWLEDGE | SKILLS | VALUES |
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| 10.7 | TRAVEL GRAPHS | $\begin{aligned} & 10.7 \\ & 10.7 \end{aligned}$ | Distance time graphs Velocity Time graphs | 10.7.1. <br> 12.2.2. <br> 12.2.2. <br> 12.2.2. <br> 10.7.2. | Compute average speed, distance and time <br> Determine acceleration and retardation/deceleration Draw travel graphs Calculate the distance under a velocity time graph Relate area under the graph to distance travelled | - Scalar and vector quantities <br> - Average speed <br> - Distance/displacement <br> - Acceleration and deceleration/retardation <br> - Drawing travel graphs <br> - Distance/area under a velocity time graph <br> - Concept of similarity <br> - Explaining why the area under the graph represents distance travelled | - Identification of Scalar and vector quantities <br> - Computation of average speed, distance and time using travel graphs. <br> - Relation between area under the graph to distance travelled. | - Curiosity in using travel graphs. <br> - Awareness of vector and scalar quantities. <br> - Appreciation of relating area under the graph to distance travelled |
|  | SOCIAL <br> AND <br> COMMERCI <br> AL <br> ARITHMETI <br> C | 10.7.1 | Investments | $10.1$ | Carry out calculations that involve Shares, dividends and investment Bonds | - Shares, dividends and Investment Bonds | - Interpretation of Shares, dividends and Investment Bonds. <br> - Calculations involving Shares, dividends and Investment Bonds. | - Appreciation of Shares, dividends and Investment Bonds. |
| 10.8 | BEARINGS | $10.4$ | Bearings and Scale Drawing | $\begin{gathered} 10.4 .4 .1 \\ 10.4 .4 .2 \end{gathered}$ | Draw/sketch diagrams to represent position and direction Use bearing and scale drawing in real life | - Scale drawing <br> - Three figure bearings <br> - Solving problems involving bearing and scale drawing from real life problems <br> - Angles | - Communication through diagrams to represent position and direction <br> - Computation involving bearing | - Awareness of bearing and scale drawing <br> - Appreciation of bearings. |


| TOPIC | SUBTOPICS | SPECIFIC OUTCOMES | KNOWLEDGE | SKILLS | VALUES |
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|  |  |  | - Measuring instruments | and scale drawing. <br> - Application of bearing and scale drawing from real life problems. |  |
| 10.9 SYMMETRY | 11.5.2 Symmetry of solids | 10.9 .1 Determine order of <br> rotational symmetry <br> 10.9 .2 Determine symmetry of <br> solids <br> 10.9 .3 Determine plane <br> symmetry | - Point, Rotational and Plane Symmetry <br> - Centre of rotation <br> - Order of symmetry in three dimension <br> - Plane and axis of symmetry | - Identification of symmetry of solids. <br> - Determination of plane symmetry | - Awareness of order of symmetry in three dimensions |
| $\begin{aligned} & \text { 10.10 } \text { COMPUTER } \\ & \text { AND } \\ & \text { CALCULAT } \\ & \text { OR } \end{aligned}$ | 10.10.1 Functions on a Calculator 10.10.2 Basic components of a computer <br> 10.2.2 Algorithms <br> 10.2.3 Methods of implementin g an algorithm | 10.2.1.1 Demonstrate the use of different functions on a calculator <br> 10.10.2.1 Describe components of a computer <br> 10.2.2.1 Describe various methods of implementing an algorithm <br> 10.2.3.1Outline problem solving stages | - Using different functions on a calculator <br> - Describing Components of a computer (i.e. Input, Process and Output Parts/devices) <br> - Definition of an algorithm <br> - Algorithm (sequence , decision loops) <br> - Methods of implementing an algorithm (flow charts and pseudo codes) <br> - Stages of problem solving (define a problem , analysis method of solution, write a computer program, | - Identification of basic components of a computer. <br> - Interpretation of functions on a calculater <br> - Modelling of simple algorithms <br> - Implementation of algorithms in programming. <br> - Coding simple computer programs. | - Logical thinking in designing flow charts. <br> - Appreciation of use of compute and calculator |


| TOPIC | SUBTOPICS | SPECIFIC OUTCOMES | KNOWLEDGE | SKILLS | VALUES |
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|  |  |  | document the program) |  |  |

## GRADE 11

## General Outcomes

- Provide clear mathematical thinking and expression in the learner
- Develop the learners' mathematical knowledge and skills
- Enrich the learners' understanding of mathematical concepts in order to facilitate further study of the discipline
- Build up an appreciation of mathematical concepts so that the learner can apply these for problem solving in everyday life.
- Enable the learner represent, interpret and use data in a variety of forms
- Inculcate a desire to develop different career paths in the learners


## Key Competences

- Assimilate necessary mathematical concepts for use in everyday life such as environment and other related disciplines.
- Thank mathematically and accurately in problem solving skills and apply these skills to formulate and solve mathematical and other related problems.
- Develop necessary skills needed to apply mathematical concepts and skills in other disciplines.
- Produce imaginative and creative work from mathematical concepts and ideas.
- Develop abilities and ideas drawn from mathematics to reason logically, communicate mathematically, and learn independently without too much supervision (self-discipline).
- Development positive attitudes towards mathematics and use it in other subjects such as science and technology.
- Apply mathematical tools such as information and communication technology in the learning of other subjects.
- Use mathematics for enjoyment and pleasure.
- Develop understanding of algebra, geometry, measurements and shapes.

| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11.1 <br> APPROXIMAT IONS | 11.11.5 Relative and absolute error | 11.11.5.1 Work with relative and absolute errors | - Relative error <br> - Limits <br> - Absolute error <br> - Tolerance <br> - Percentage error <br> - Estimation | - Interpretation of relative and absolute error. <br> - Computation of absolute and relative error. <br> - Comparison of measurements. | - Accuracy in finding relative and absolute error. |
| $\begin{aligned} & 11.2 \text { SEQUENCES } \\ & \text { AND SERIES } \end{aligned}$ | 11.2.1 Arithmetic progression <br> 11.2.2 Geometric progression | 11.2 .3 .1 Identify an arithmetic <br> progression (AP) <br> 11.2.3.2 Find the nth term of the <br> AP <br> 11.2.3.3 Find the sum of an AP <br> 11.2.3.4Find the arithmetic mean  <br> 11.2.4.1 Identify a geometric <br> progression (GP) <br> 11.2.4.2 Find the nth term of a GP <br> 11.2.4.3 Find the geometric mean  <br> 11.2.4.4Find the sum of a <br> geometric progression  <br> 11.2.4.5Find the sum to infinity of <br> a Geometric progression  <br> 1  | - Arithmetic and Geometrical Progressions. <br> - The nth terms of AP and GP <br> - Sums of APs and GPs <br> - Arithmetic and geometric means <br> - Sum to infinity of a Geometric progression | - Identification of arithmetic and geometrical Progressions. <br> - Ordering of Arithmetic and Geometrical Progressions. <br> - Computation of Arithmetic and Geometrical Progressions. | - Accuracy in computing progressions. <br> - Appreciation of the nth term of the progression. <br> - Prediction of the nth term. |
| 11.3 COORDINAT <br>  E <br>  GEOMETRY | 11.6.1 Length of a straight line between two points <br> 11.6.2 The mid point <br> 11.6.3 Gradient <br> 11.6.4 Equation of a straight line | 11.6.1.1 Calculate the length of a straight line <br> 11.6.1.2 Calculate the mid-point of two points <br> 11.6.1.3 Calculate the gradient of a line segment <br> 11.6.4.1 Find the equation of a straight line | - Length (distance formula) <br> - Mid point <br> - Gradient <br> - Gradient point form <br> - Gradient Intercept form | - Interpretation of distance and gradient formula. <br> - Calculation of gradient of a line segment. | - Curiosity in using distance and gradient formula. <br> - Recognition of distance and gradient formula. |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
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|  | $\begin{array}{cl} \hline \text { 11.6.5 } & \text { Parallel and } \\ & \text { perpendicular } \\ \text { lines } \end{array}$ | 11.6.5.1 Find the gradients of parallel and perpendicular lines <br> 11.6.5.2 Use gradients of parallel and perpendicular lines to find equations | - Double intercept form <br> - Parallel lines <br> - Perpendicular lines |  |  |
| 11.4 RELATIONS <br>  AND <br>  FUNCTIONS | $\begin{array}{ll} \text { 11.14.9 Inverse } \\ \text { functions } \\ \text { 11.4.3 } & \text { Composite } \\ \text { functions } \\ \text { 11.14.11 Application } \end{array}$ | 11.14.9.1 Find inverses of one- toone functions <br> 11.4.3.1 Simplify composite functions <br> 11.14.11.1 Solve problems involving linear functions | - Formula, functional notation, set builder notation <br> - Inverse functions <br> - Composite functions <br> - Problems involving linear functions | - Identification of inverse of a function. <br> - Representation of composite functions. <br> - Problem solving involving linear functions. | - Logical thniking in solving inverse and copmosite functions. <br> - Appreciation of functions. |
| 11.5 QUADRATIC FUNCTIONS | 11.5.1 Introduction to <br>  Quadratic <br>  Functions | 11.5.1.1 Explain the quadratic function and its graph <br> 11.5.1.2 Sketch the graph of a quadratic function | - Meaning of quadratic function and its graph <br> - Sketching the graph <br> - Maximum and minimum Roots/zeros | - Identification of a quadratic function. <br> - Interpretation of Maximum and minimum of function. <br> - Drawing of function graphs. | - Neatness in sketching graphs. <br> - Logical thinking in determining the turning points. <br> - Accuracy in finding the roots. |
| 11.6 QUADRATIC EQUATIONS | 11.6.2Introduction to <br> 11.6.2Quadratic <br> equations <br> Solutions of <br> quadratic | 11.3.1.2 Explain the meaning of the quadratic equation <br> 11.3.3.2 Solve quadratic equations by graphical method <br> 11.6.1.2 Solve quadratic equations | - Meaning of quadratic equation <br> - Solving quadratic equations by Factorisation, | - Identification of method of quadratic <br> - Computation of quadratic | $\bullet$ Logical thinking in computing quadratic equations. <br> - Accuracy in |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
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|  | equations | using factorisation method <br> 11.3.2.1 Solve quadratic equations using completing of square method <br> 11.3.3.1 Solve quadratic equations using quadratic formula method <br> 11.3.4.1 Apply quadratic equations to solve real life problems | graphical method, completion of squares and quadratic formula <br> - Application of quadratic equations | equations using various methods. | finding quadratic roots. |
| 11.7 VARIATION | 11.7.1 Introduction to <br>  variation <br> 11.7.2 Direct and <br>  Inverse <br> 11.7.3 Variation <br>  Joint and Partial <br> 11.7.4 Garaation <br> 11.7.5 Applications | 11.15.1.1 Describe variation <br> 11.15.2.1 Distinguish between direct and inverse variation <br> 11.15.3.1 Distinguish between joint and partial variation <br> 11.15.4.1 Draw and Interpret graphs of variation <br> 11.7.5.1 Solve problems involving variations | - Describing variation (Notation and Constant) <br> - Distinguishing between direct and inverse variation <br> - Distinguishing between Joint and Partial variation <br> - Graphs of variation <br> - Solving problems involving variations | - Interpretation of variation <br> - Problem solving involving variations <br> - Comparison between joint and partial variation. | - Apprecation of variation in <br> - Logica thinking in calcualating |
| $\begin{array}{\|ll\|} \hline 11.8 \text { CIRCLE } \\ \text { THEOREMS } \end{array}$ | 11.7.3 Properties of a <br> circle <br> 11.7.2 Angle properties | 11.7.3.1 Analyse the parts of a <br> circle <br> 11.7.2.1 Solve problems using <br> angle properties of a <br> circles  | - Parts a circle (chord, segment, arc, sector, radius, diameter) <br> - Angle in the same segment <br> - Angle at the centre twice one at the circumference <br> - Angle in a semicircle <br> - Cyclic quadrilateral | - Identification of parts of a circle (chord, segment, arc, sector, radius, diameter) <br> - Computation involving angle properties of a circle. <br> - Interpretation of | - Curiosity I using circle theorems. <br> - Appreciation of angle property of a circle. |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
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|  |  |  | (opposite sides) <br> - Alternate segments <br> - Tangent properties of a circle <br> - External angle of a cyclic Quadrilateral equal to the opposite interior angle | circle theorems. |  |
| 11.9 <br> CONSTRUCT <br> ION AND <br> LOCI | 11.9.1 Construction <br> 11.9.2 Locus <br> 11.9.3 Loci in two dimensions <br> 11.9.4 Loci in three dimension | 11.9.1.1 Construct line and angle <br> bisectors <br> 11.9.1.2 Explain the meaning of <br> 10cus <br> 11.9.1.3 Lescribe locus of point in <br> two and three dimensions <br> 11.9.1.4 Construct locus of point <br> in two dimensions | - Line and angle bisectors <br> - Finding the centre of circle <br> - Constructing a tangent from a point to a circle <br> - meaning of Locus <br> - Locus of points in two and three dimensions (equidistant from a Point and two fixed points, from two intersecting line, from a Straight line) <br> - Locus of points which subtends a constant angle <br> - Locus of points such that the area of triangles is constant | - Identification of loci of points. <br> - Construction locus of point in two and three dimensions. | - Accuracy in construction. <br> - Neatness in constructing lines and points. <br> - Appreciation of loci. |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
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| $\begin{array}{ll} 11.10 & \\ & \text { TRIGONOME } \\ & \text { TRY } \end{array}$ | 11.10.1 Introduction to <br> Trigonometry <br> 11.10 .1 Trigonometric <br> ratios <br> 11.10 .4 Sine and Cosine <br> rules <br> 11.10 .5 Area of a <br> triangle <br>   |  | - Sine, cosine and tangent ratios on a right angled triangle (Opposite, adjacent and hypotenuse sides) <br> - Three trigonometric ratios in quadrants <br> - Sides and angles of right angled triangles using the three trigonometric ratios <br> - Special angles ( $60,{ }^{0} 45^{\circ}$ and $30^{\circ}$ ) <br> - Finding sides and angles of non right angled triangles using the sine and cosine rule. <br> - Calculating area of a non right angled triangle using the sine rule. <br> - Using of Mathematical tables and scientific calculators <br> - Determining signs of the three trigonometric ratios | - Comparison <br> - Identification of trigonometric ratios. <br> - Interpretation Opposite, adjacent and hypotenuse sides <br> - Computation of sides and angles of a right angled triangle. <br> - Determination of the signs of the three trigonometric ratios in respective quadrants <br> - Application of trgonometry in rel life situations. | - Appreciation of trigonometry ratios. <br> - Curiosity in using cosine and sine rules. <br> - Logical thinking in computing trigonometric problems. |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | in the quadrants <br> - Graphs of $(y=\sin \theta$, $y=\cos \theta$ and $y=\tan$ $\theta$ ) <br> - Application of trigonometry (Include three dimensional figures) (Include: Bearings) |  |  |
| 11.12 <br> MENSURATION | 11.12.1 Area 11.8.2 Volume | 11.12.1.1 Calculate the area of a sector <br> 11.12.1.2 Calculate surface area of three dimensional figures <br> 11.8.3.1 Calculate volume of prisms <br> 11.8.3 4 Solve problems involving area and volume | - Area of a sector <br> - Surface area of three dimensional figures (pyramid and cone) <br> - Volume of solids (cone, rectangular and triangular pyramids. Include: frustum) <br> - Solving problems involving area and volume. | - Interpretation of sector of a circle. <br> - Computation of the area and volume of figures. <br> - Relation between area and volume. | - Appreciation of area and volume of figures. <br> - Accuracy in calculations of volume and area. |
| $\begin{array}{\|ll} \hline 11.13 & \\ \mathrm{Y} & \text { PROBABILIT } \end{array}$ | 11.12.3 Laws of <br> probability <br> 11.12 .4 Tree <br>  <br>  <br> Diagrams and <br> grid | $\left.\begin{array}{\|ll}\text { 11.12.3.1 } & \begin{array}{l}\text { Compute probabilities } \\ \text { using the laws of } \\ \text { probability }\end{array} \\ \text { 11.12.4.1 } & \begin{array}{l}\text { Calculate probabilities } \\ \text { using tree diagrams and } \\ \text { grids. }\end{array} \\ \text { 11.12.4.2 } & \begin{array}{l}\text { Calculate probabilities of } \\ \text { mutually exclusive events }\end{array} \\ \text { and compound events }\end{array}\right\}$ | - Addition and Multiplication Laws <br> - Calculating probabilities using tree diagrams and grids. <br> - Calculating expected values, Independent and dependent events, Mutually | - Computation of probabilities using the laws of probability <br> - Interpretation tree diagrams and grids to calculate probabilities. <br> - Communication <br> - Analysis of | - Curiosity in using laws of probabilities. <br> - Logical thinking in calculating probabilities. |


| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | independent events <br> 11.12.4.5 Apply probability to real life problems | exclusive events, conditional events and Compound events. <br> - Continuous sample space. | mutually exclusive events, compound and independent events. |  |
| 11.14 STATISTIC | 11.14.2 Cumulative frequency tables <br> 11.14.3 Measures of dispersion | 12.7.2.1 Construct cumulative <br> frequency tables using <br> grouped and ungrouped <br> data <br> 12.7.2.2 Draw cumulative <br> frequency curves <br> 12.7.2.3 Draw relative cumulative <br> curves <br> Calculate the range, inter <br>  quartile range, and semi <br> inter quartile range <br> 12.7.3.3 Calculate the percentiles <br> 12.7.3.4Calculate variance and <br> standard deviation for <br> ungrouped and grouped <br> data <br>   | - Constructing Cumulative frequency tables <br> - Drawing Cumulative frequency curves (ogive) <br> - Drawing Relative cumulative frequency curves <br> - Calculating the range, inter quartile range, semi inter quartile range and Percentiles <br> - Calculating variance and standard deviation for ungrouped and grouped data | - Drawing cumulative tables and frequency curves. <br> - Computation of measures of dispersion. <br> - Interpretation of cumulative curves. | - Logical thinking in computation of measures of dispersion <br> - Appreciation of cumulative and frequency curves. |

## GRADE 12

## General Outcomes

- Provide clear mathematical thinking and expression in the learner
- Develop the learners' mathematical knowledge and skills
- Enrich the learners' understanding of mathematical concepts in order to facilitate further study of the discipline
- Build up an appreciation of mathematical concepts so that the learner can apply these for problem solving in everyday life.
- Enable the learner represent, interpret and use data in a variety of forms
- Inculcate a desire to develop different career paths in the learners


## Key Competences

- Assimilate necessary mathematical concepts for use in everyday life such as environment and other related disciplines.
- Thank mathematically and accurately in problem solving skills and apply these skills to formulate and solve mathematical and other related problems.
- Develop necessary skills needed to apply mathematical concepts and skills in other disciplines.
- Produce imaginative and creative work from mathematical concepts and ideas.
- Develop abilities and ideas drawn from mathematics to reason logically, communicate mathematically, and learn independently without too much supervision (selfdiscipline).
- Development positive attitudes towards mathematics and use it in other subjects such as science and technology.
- Apply mathematical tools such as information and communication technology in the learning of other subjects.
- Use mathematics for enjoyment and pleasure.
- Develop understanding of algebra, geometry, measurements and shapes.

| TOPIC | SUB TOPIC | SPECIFIC OUTCOME | KNOWLEDGE | SKILLS | VALUES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12.1 GRAPHS OF <br>  FUNCTIONS | 12.1.1 Cubic <br> functions <br> 12.1.2 Inverse <br> functions  | 12.1.1.1 Draw graphs of cubic functions <br> 12.1.1.2 Use graphs to find solutions <br> 12.1.1.3 Determine gradients of curves <br> 12.1.1.4 Estimate areas under curves <br> 12.1.2.1 Draw graphs of inverse functions <br> 12.1.2.2 Application of graphs of functions | - Drawing Graphs of cubic functions <br> - Finding Zeros of the function, Solutions of graphs <br> - Determining Gradients of curves <br> - Turning points and their nature (Maximum and minimum) <br> - Area under the graph (Counting square, Trapezium) <br> - Drawing Graphs of inverse functions <br> - Exponential graphs <br> - Applying graphs of functions | - Identification of a cubic function. <br> - Interpretation of gradients and areas under curves. <br> Drawing graphs of cubic and inverse functions. | - Neatness in sketching graphs. <br> - Logical thinking in determining area under the curve. <br> - Accuracy in finding the turning points. |
| 12.2 LINEAR <br> PROGRAMMI <br> NG | 12.2.1 Linear programming | 12.2.1.2 Draw graphs of linear equations and inequations in one and two variables (as a recap) <br> 12.2.1.3 Shade the wanted and unwanted regions <br> 12.2.1.3 Describe the wanted or unwanted regions. <br> 12.2.1.3 Determine maximum | - Drawing graphs of linear equations and inequations in one and two variables (as a recap) <br> - $\quad$ Shading the wanted and unwanted regions <br> - Describing the wanted or unwanted region <br> - Finding Values in the feasible region | - Interpretation of the wanted or unwanted regions. <br> - Shading of the unwanted region. <br> - Determination of maximum and minimum values. | $\bullet$ Logical thinking in finding the wanted region. <br> - Planning when using graph paper. |


|  |  |  | and minimum values <br> 12.2.1.4 Use the search line to determine the maximum and minimum values <br> 12.2.1.5 Apply knowledge of linear programming in real life | - Using the Search line to determine the maximum and minimum values <br> - Applying knowledge of linear programming in real life | - Application of linear programming in real life situation. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12.3 | TRAVEL GRAPHS | $\begin{array}{ll} \hline \text { 12.3.1 } & \text { Velocity - } \\ & \text { time graphs } \\ & \text { (Curves) } \end{array}$ | 12.3.1.1 Calculate the displacement in a velocity - time graph | - Distance/area under the graph in a velocity time graph | - Representation of velocity-time graphs. <br> - Interpretation of displacement in a velocity time graph. | $\bullet$ Curiosity in using velocity-time graphs |
| $12.4$ | VECTORS IN TWO DIMENSION S | 12.4.1 Introduction to vectors <br> 12.4.2 Addition and subtraction <br> 12.4.3 Translations <br> 12.4.4 Scalar multiplication <br> 12.4.5 Collinearity <br> 12.4.6 Vector geometry | 12.4.1.1 Describe a vector <br> 12.4.1.2 Represent and <br> denote a vector <br> 12.4.2.1 Add and subtract <br> vectors <br> 12.4.3.1 Apply translations <br> on vectors and find <br> magnitude <br> 12.4.4.1 Multiply vectors by <br> scalars <br> 12.4.5.1 Determine <br> collinearity of <br> points <br> 12.4.6.1 Solve geometrical <br> problems involving <br> vectors | - Describing a vector (direction and magnitude) <br> - Zero and Free vectors <br> - Representing and denoting <br> - Adding and subtracting vectors (triangular and parallelogram laws) <br> - Resultant vectors <br> - Multiplying vectors by scalars <br> - Translation (Position vectors) <br> - Component form <br> - Calculating Magnitude/Modulus of | - Representation of vector quantities <br> - Computation of vector related problems <br> - Application of vector in Problem solving | - Appreciation of sense of direction <br> - Logical thinking in solving vector problems. <br> - Creativity in design |


|  |  |  | vectors <br> - Collinearity and parallelism <br> - Ratios (Mid - point theorem) <br> - Vector geometry |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12.5 <br> GEOMETRICA <br> L <br> TRANSFORMATIO NS | 12.5.1 Introduction to <br>  transformation <br> 12.5.2 Translation <br> 12.5.3 Reflection. <br> 12.5.4 Rotation. <br> 12.5.5 Enlargement <br> 12.5.6 Stretch <br> 12.5.7 Shear <br> 12.5.8 Combined <br>  transformations | $\left.\begin{array}{\|l\|}\text { 12.5.1.1 } \\ \text { 12.5.2.1 } \\ \begin{array}{l}\text { Explain the concept } \\ \text { of transformation }\end{array} \\ \text { Use a column vector } \\ \text { to translate an } \\ \text { object }\end{array}\right\}$ | - Explaining the concept of transformation (Object and Image) <br> - Translation ( Translation vector, Mediator) <br> - Reflection ( mirror lines and matrices of reflections) <br> - Rotations (by construction and matrix methods) <br> - Rotations (Finding centre, angle and direction ) <br> - Finding matrix of rotation <br> - Enlargement (by construction and matrix methods) <br> - Finding the centre, scale factor and matrix of enlargement <br> - Stretch (by construction and matrix methods) <br> - Finding the centre, scale factor, invariant line | - Interpretation the concept of transformation <br> - Comparison between different forms of transformation. <br> - Computation involving transformations. | - Appreciation of transformations <br> - Logical thinking in solving transformations. <br> - Creativity in designing. |


|  |  |  | and matrix of stretch <br> - Shear (by construction and matrix methods) <br> - Finding the shear factor, invariant line and matrix of shear <br> - Area scale factor <br> - Determinant of a matrix <br> - Inverse transformations |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12.6 EARTH <br>  GEOMETRY | 12.6.1 Introduction <br> to Earth <br> 12.6.2 <br> Geometry <br> Small and <br> great circles  <br> 12.6.3 Latitudes and <br> Longitudes <br> 12.6.4 Distance <br> along latitudes <br> and longitudes <br>  Speed in <br> Knots and <br> time | 12.6.1.1 Explain the concept of Earth Geometry <br> 12.6.2.1 Distinguish between small and great circles <br> 12.6.3.1 Calculate distance along parallels of latitudes and longitude in kilometres and nautical miles <br> 12.6.3.2 Calculate the shortest distance between two points on the surface of the earth <br> 12.6.5.1 Calculate speed in knots and time | - Explaining the concept of Earth Geometry and its significance <br> - Southern and Northern hemispheres ( South and North Poles) <br> - Great Circles(the equator and all longitudes) <br> - The Greenwich and Equator <br> - Small Circles(latitudes) <br> - Centre of the earth <br> - Length ,chord , arc and sector <br> - Angular distance <br> - Line of axis of the Earth <br> - Circumference of the earth <br> - Standard units of distances in degrees and miles ( $1^{\circ}$ of latitude represents 60 nautical miles/or 110.9 Km ) | - Application of the relationship of earth geometry in real life. <br> - Computation of distances of latitudes and longitudes. <br> - Location of points on the globe. | - Appreciation of the concept of earth geometry. <br> - Curiosity in exploring earth geometry. <br> - Team work through cooperative learning |


|  |  |  | - Conversion of distance in kilometre and nautical mile <br> - Longitude and time <br> - Greenwich Mean Time <br> - Solving problems involving Earth Geometry in real life |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12.7 <br> INTRODUCT <br> ION TO CALCULUS | 12.7.1 Differentiation 12.7.2 Integration | 12.7.1.1 Explain concept of <br> differentiation <br> 12.7.1.3 Differentiate <br> functions from first <br> principles. <br> 12.7.1.4 Use the formula for <br> differentiation <br> 12.7.1.8 Calculate equations <br> of tangents and <br> normals <br> 12.7.2.1 Explain integration <br> 12.7.2.2 Find Indefinite <br> integrals <br> Evaluate simple <br> definite integrals <br> 12.7.2.3 Find the area under <br> the curve <br>   | - Explaining the concept of differentiation <br> - Differentiating functions from first principles (Limits) <br> - Product rule; chain rule and quotient rule $\left(\mathrm{y}=\mathrm{ax}^{\mathrm{n}} ; \frac{d y}{d x}=\mathrm{nax}^{\mathrm{n}-1}\right)$ <br> - Indefinite integrals <br> - Arbitrary constant <br> - Definite integrals <br> - Stationary points <br> - Secant <br> - Tangents <br> - Normal <br> - Explain integration as the reverse of differentiation <br> - Rule of integration $\left(\frac{d y}{d x}\right.$ $=a x^{n} ; \quad \int a x^{n} d x=$ $\frac{a x^{n+1}}{n+1}+c$ <br> - Area under the curve | - Interpretation of differentiation and integration <br> - Application of definite integrals. <br> - Estimation of area under the curve. | - Appreciation of calculus. <br> - Curiosity in differentiating and integrating. <br> - Critical thinking in using rules for differentiation and integration. |



## GRADES 10 TO 12 "0" LEVEL MATHEMATICS SCOPE AND SEQUENCE

The table below shows the coverage of the syllabus in Mathematics from Grades 10 to 12 . It is important for a teacher to refer to this table from time to time to know the knowledge that the learners already have or need to have at various levels of learning of the subject.

| DOMAIN | SPPCIFIC OUTCOME |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | GRADE 10 | GRADE 11 | GRADE 12 |


| - ALGEBRA | - SETS | - Carry out operations on sets. <br> - Apply higher operations on sets | $\bullet$ | - |
| :---: | :---: | :---: | :---: | :---: |
|  | - LINEAR <br> PROGRAMMING | - Aplo | - | - Draw graphs of linear equations and inequations in one and two variables (as a recap) <br> - Shade the wanted and unwanted regions <br> - Describe the wanted or unwanted regions. <br> - Determine maximum and minimum values <br> - Use the search line to determine the maximum and minimum values <br> - 12.2.1.5 Apply knowledge of linear programming in real life |
|  | - ALGEBRA | - Expand and simplify | - | $\bullet$ - |



|  |  |  | equations to solve real life problems |  |
| :---: | :---: | :---: | :---: | :---: |
|  | - VARIATION | $\bullet$ | - Describe variation <br> - Distinguish between direct and inverse variation <br> - Distinguish between joint and partial variation <br> - Draw and Interpret graphs of variation <br> - Solve problems involving variations | $\bullet$ |
| - FUNCTIONS | - QUADRATIC FUNCTIONS | - | - Explain the quadratic function and its graph <br> - Sketch the graph of a quadratic function | $\bullet$ |
|  | - INTRODUCTION TO CALCULUS | $\bullet$ | - | - Explain concept of differentiation <br> - Differentiate functions from first principles. <br> - Use the formula for differentiation <br> Calculate equations of tangents and normals <br> - Explain integration <br> - Find Indefinite integrals <br> - Evaluate simple definite integrals <br> - Find the area under the curve |


| - GEOMETRY | - COORDINATE GEOMETRY | $\bullet$ | - Calculate the length of a straight line <br> - Calculate the midpoint of two points <br> - Calculate the gradient of a line segment <br> - Find the equation of a straight line <br> - Find the gradients of parallel and perpendicular lines <br> - Use gradients of parallel and perpendicular lines to find equations | $\bullet$ |
| :---: | :---: | :---: | :---: | :---: |
|  | - VECTORS IN TWO DIMENSIONS | $\bullet$ | $\bullet$ | - Describe a vector <br> - Represent and denote a vector <br> - Add and subtract vectors <br> - Apply translations on vectors and find magnitude <br> - Multiply vectors by scalars <br> - Determine <br> - collinearity of points <br> - Solve geometrical problems involving vectors |
|  | - SIMILARITY AND CONGRUENCY | - Calculate the scale on a map <br> - Calculate length and area using | $\bullet$ | $\bullet$ |


|  |  | a given scale and vice versa <br> - Calculate areas and volumes of similar figures <br> - Apply ratio, proportion, to solve problems on similarity and congruence |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | - GEOMETRICAL TRANSFORMATIONS | $\bullet$ |  | - Explain the concept of transformation <br> - Use a column vector to translate an object <br> - Reflect objects by different methods <br> - Rotate objects by different methods <br> Enlarge objects by different methods <br> - Stretch objects by different methods <br> - Shear objects by different methods <br> - Solve problems involving combined transformations <br> - Find area scale factors of a stretch by determinant method |
|  | - 12.6 EARTH GEOMETRY | - |  | - Explain the concept of Earth Geometry <br> - Distinguish between small and great circles <br> - Calculate distance along parallels of |


|  |  |  |  | latitudes and longitude in kilometres and nautical miles <br> - Calculate the shortest distance between two points on the surface of the earth <br> - Calculate speed in knots and time |
| :---: | :---: | :---: | :---: | :---: |
|  | - BEARINGS | - Draw/sketch diagrams to represent position and direction <br> - Use bearing and scale drawing in real life | $\bullet$ | - |
|  | - CIRCLE THEOREMS | - | - Analyse the parts of a circle <br> - Solve problems using angle properties of a circles <br> - Solve problems involving tangent properties | $\bullet$ |
|  | - SYMMETRY | - Determine order of rotational symmetry <br> - Determine symmetry of solids <br> - Determine plane symmetry | $\bullet$ | $\bullet$ |
|  | - CONSTRUCTION AND LOCI | $\bullet$ | - Construct line and angle bisectors <br> - Explain the meaning of Locus | $\bullet$ |




|  |  |  |  | velocity - time graph |
| :---: | :---: | :---: | :---: | :---: |
|  | - TRAVEL GRAPHS | - Compute average speed, distance and time <br> - Determine acceleration and retardation/deceleration <br> - Draw travel graphs <br> - Calculate the distance under a velocity time graph <br> - Relate area under the graph to distance travelled | - | - |
|  | $\begin{aligned} & \hline \text { - SOCIAL AND } \\ & \text { COMMERCIAL } \\ & \text { ARITHMETIC } \\ & \hline \end{aligned}$ | - Carry out calculations that involve Shares, dividends and investment Bonds | - | - |
|  | - SEQUENCES AND SERIES | - | - Identify an arithmetic progression (AP) <br> - Find the nth term of the AP <br> - Find the sum of an AP <br> - Find the arithmetic mean <br> - Identify a geometric progression (GP) <br> - Find the nth term of a GP <br> - Find the geometric mean <br> - Find the sum of a geometric progression <br> - Find the sum to infinity of a Geometric | - |



|  |  |  | - Simplify composite functions <br> - Solve problems involving linear functions |  |
| :---: | :---: | :---: | :---: | :---: |
| - STATISTICS | - STATISTIC | - | - Construct cumulative frequency tables using grouped and ungrouped data <br> - Draw cumulative frequency curves <br> - Draw relative cumulative curves <br> - Calculate the range, inter quartile range, and semi inter quartile range <br> - Calculate the percentiles <br> - Calculate variance and standard deviation for ungrouped and grouped data | - |

